

## Unit 1: Linear Systems - Quiz #2

LS3	I am learning to use graphs to solve a pair of linear equations simultaneously.	/5
-----	---	----

1. Solve the following linear system graphically. State the P.O.I. (5 marks)

①

$$y = 2x - 4$$

②

$$3x + y = 6$$

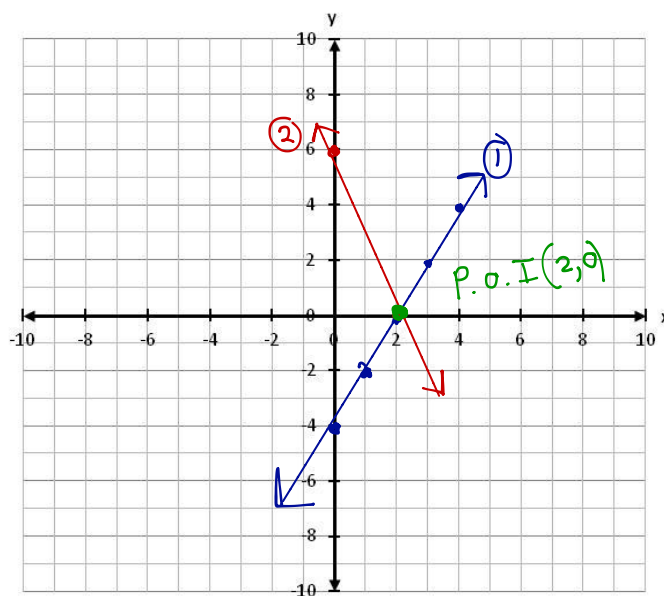
$$y \text{ Int. } y = 6$$

$$x = 0$$

$$x \text{ Int. } y = 0$$

$$3x = 6$$

$$x = 2$$



LS1	I am learning to model problems involving the intersection of straight lines using tables, graphs, and equations.	/4
-----	---	----

1. Mrs. Neave needs 200 g of chocolate that is 86% cocoa for a cake recipe. She has one kind of chocolate that is 99% cocoa and another kind that is 70% cocoa. How much of each kind of chocolate does he need to make the cake?

- (a) Assign each unknown in the situation a variable, explaining in a statement what the chosen variable represents. (2 marks)

Let  $n$  represent the amount of 99% cocoa  
 Let  $s$  represent the amount of 70% cocoa.

- (b) Represent this situation with a linear system. (2 Equations) (2 marks)

①

$$n + s = 200$$

②

$$0.99n + 0.7s = 0.86(200)$$

$$0.99n + 0.7s = 172$$

LS2	I am learning to solve systems of linear equations involving variables using an algebraic method.	/6
-----	---	----

2. Solve the following linear system algebraically (substitution method). Show all of your work. (6 marks)

$$\textcircled{1} \quad 2x - 5y = -27$$

$$\textcircled{2} \quad x + 3y = 3 \quad \text{Isolate } x \text{ in } \textcircled{2}$$

$$x = 3 - 3y \quad \textcircled{3}$$

Sub.  $\textcircled{3}$  into  $\textcircled{1}$

$$2x - 5y = -27$$

$$2(3 - 3y) - 5y = -27$$

$$6 - 6y - 5y = -27$$

$$6 - 11y = -27$$

$$-11y = -27 - 6$$

$$-11y = -33$$

$$\frac{-11}{-11} \quad \frac{-11}{-11}$$

$$\boxed{y = 3}$$

→ sub into  $\textcircled{3}$

$$x = 3 - 3y$$

$$x = 3 - 3(3)$$

$$x = 3 - 9$$

$$\boxed{x = -6}$$

P.O.I.  $(-6, 3)$

Pg. 39 #7

$$\begin{aligned} & 250 \text{ g} \\ & 500 \text{ g} \\ & (( 186.5 \text{ kg} \\ & = 186.5 \times 1000 \\ & = 186500 \text{ g} \end{aligned}$$

Let  $t$  represent # of 250g jars  
 Let  $b$  represent # of 500g jars

$$\begin{aligned} \textcircled{1} \quad t + b &= 511 \\ \textcircled{2} \quad 250t + 500b &= 186500 \end{aligned}$$

Isolate  $t$  in  $\textcircled{1}$

$$t = 511 - b \quad \textcircled{3}$$

sub.  $\textcircled{3}$  into  $\textcircled{2}$

$$\begin{aligned} 250t + 500b &= 186500 \\ 250(511 - b) + 500b &= 186500 \\ 127750 - 250b + 500b &= 186500 \end{aligned}$$

$$\begin{aligned} 127750 + 250b &= 186500 \\ 250b &= 186500 - 127750 \\ 250b &= 58750 \\ b &= \frac{58750}{250} \\ b &= 235 \end{aligned}$$


$$\begin{aligned} t &= 511 - b \\ t &= 511 - 235 \\ t &= 276 \end{aligned}$$

$$\therefore \begin{array}{l} 276 \text{ } 250 \text{ g jars} \\ 235 \text{ } 500 \text{ g jars} \end{array}$$

# Big Ideas

- Equivalent Systems of Linear Equations
  - Two or more systems of linear equations that have the same solution.

P.O.I.

Handwritten blue text "P.O.I." with an arrow pointing up and to the right.

# More Big Ideas

- You can create an equivalent system of linear equations by:
  - Adding or subtracting the equations in a linear system.
  - Multiplying one or both equations of a system by a constant other than 0.

# Example

- Consider the linear system:

$$x - 3y = 2 \quad (1)$$

$$2x + y = -5 \quad (2)$$

- Add and subtract the equations to create an equivalent linear system.
- Multiply each equation in the system by a different constant to create another equivalent linear system.

$$\begin{array}{l} \textcircled{1} \quad x - 3y = 2 \\ \textcircled{2} \quad 2x + y = -5 \end{array}$$

---

$$\textcircled{3} \quad 3x - 2y = -3$$

$$\textcircled{1} \quad x - 3y = 2$$

$$\textcircled{2} \quad 2x + y = -5$$

---

$$\textcircled{4} \quad -x - 4y = 7$$

$\textcircled{1}$  &  $\textcircled{2}$  have the same P.O.I.  
as  $\textcircled{3}$  &  $\textcircled{4}$

$$\textcircled{1} \quad x - 3y = 2$$

Eqn  $\textcircled{1}$   $\times 2$

$$\textcircled{2} \quad 2x + y = -5$$

$$\textcircled{3} \quad 2x - 6y = 4$$

$$\textcircled{2} - \textcircled{3}$$

$$2x + y = -5$$

$$2x - 6y = 4$$

---

$$0 + 7y = -9$$

Eliminated  
a variable

# Consolidation

- A teacher claims that these systems of linear equations are equivalent. Is she correct?

System A	System B	System C
$3x - 2y = 2$ ① $-10x + 3y = 8$ ②	$-7x + y = 10$ $13x - 5y = -6$	$x = -2$ ✓ $y = -4$ ✓

Solve A

Isolate  $y$  in ①

$$\cancel{3x} - \cancel{3x} - 2y = 2 - 3x$$

$$\frac{-2y}{-2} = \frac{2-3x}{-2}$$

$$y = -1 + 1.5x \text{ ③}$$

③ into ②

$$-10x + 3(-1 + 1.5x) = 8$$

$$-10x - 3 + 4.5x = 8$$

$$-5.5x = 11$$

$$x = \frac{11}{-5.5}$$

$$x = -2$$

$$y = -1 + 1.5(-2)$$

$$y = -1 - 3$$

$$y = -4$$



System B

$$-7x + y = 10 \quad (1)$$

$$13x - 5y = -6 \quad (2)$$

Isolate  $y$  in (1)  $y = 10 + 7x$  (3)

Sub (3) in (2)

$$13x - 5y = -6$$

$$13x - 5(10 + 7x) = -6$$

$$13x - 50 - 35x = -6$$

$$-22x = -6 + 50$$

$$-22x = 44$$

$$x = \frac{44}{-22}$$

$$(3) \quad y = 10 + 7x$$

$$y = 10 + 7(-2)$$

$$y = 10 - 14$$
$$y = -4$$

$$x = -2$$

∴ System A, B & C are equivalent.

# Reinforcement

- Pages 46 - 48
  - #3, 4, 6, 8a

Note for 1.6 on line  
tonight.